

# Symbolic Implementation of Connectors in BIP



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ICE'09, Bologna, August 31, 2009

# Presentation outline

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- BIP
- Connectors
- Boolean encoding
- Benchmarks

# Motivation

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**Context:** *Component-based* modelling, design and validation of embedded real-time systems.

**Presently:**

- A number of *coordination mechanisms* for concurrent systems: shared variables, semaphores, regions, etc.
- Ad-hoc use and analysis methodologies.

**Our goal:** *Unified framework* for component-based modelling and design

- allowing incremental description & correctness by construction
- encompassing heterogeneity
  - synchronous and asynchronous execution
  - event and data driven computation
  - centralised and distributed implementation



# Component design by refinement

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## Three layers:

1. Component behaviour
2. Coordination
3. Data transfer

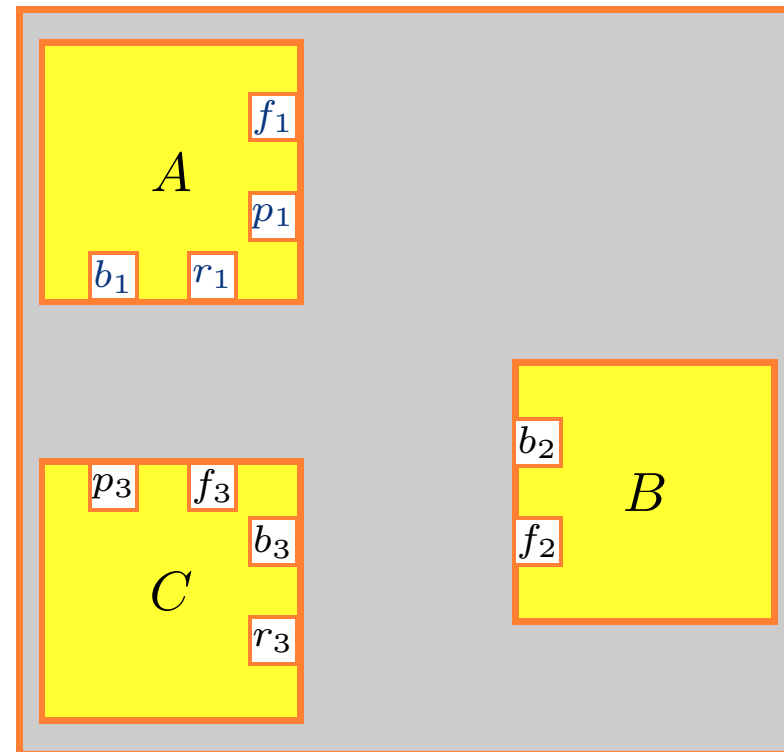


# Component design by refinement

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## Three layers:

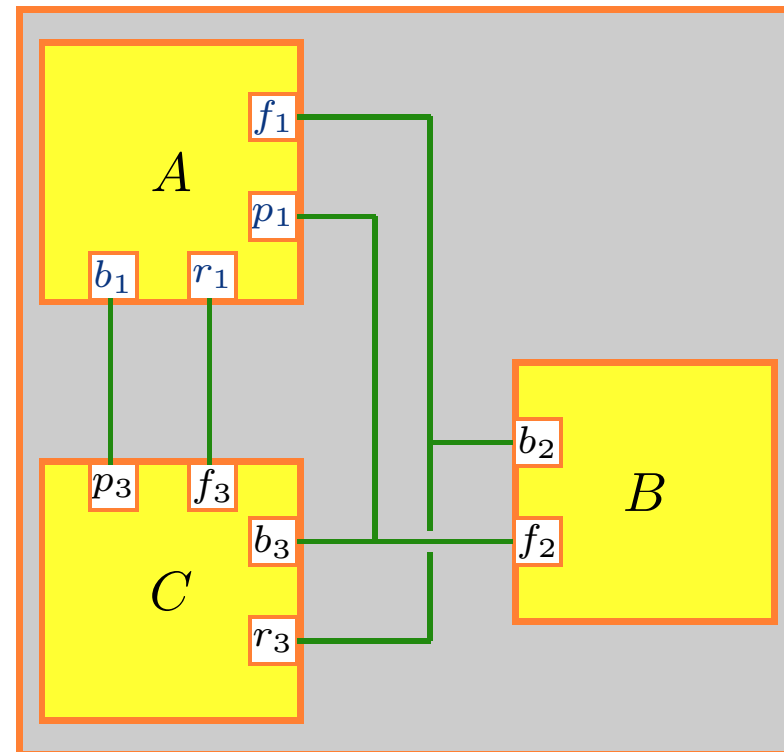
1. Component behaviour
2. Coordination
3. Data transfer



# Component design by refinement

## Three layers:

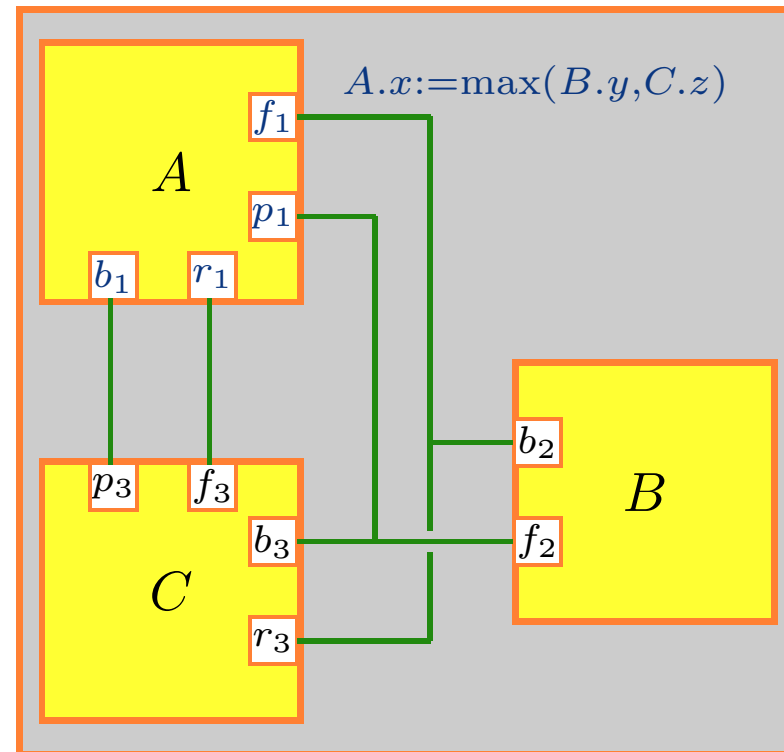
1. Component behaviour
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# Component design by refinement

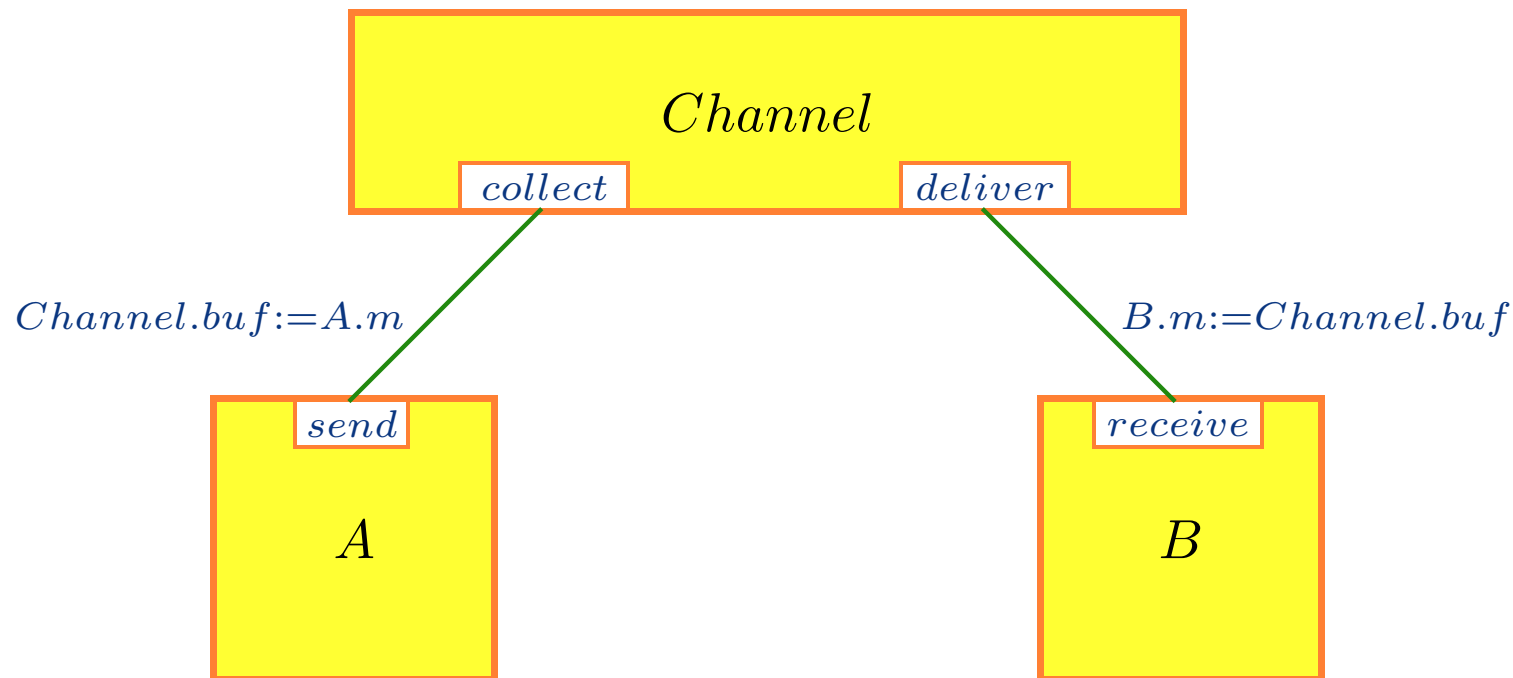
## Three layers:

1. Component behaviour
2. Coordination
3. Data transfer



# Unbuffered synchronous communication

(Not to confuse with synchronous *execution*!)



*A* sends a message *m* to *B*:

- Two synchronisations with the channel
- Each synchronisation allows a data transfer
- An explicit model of the channel behaviour



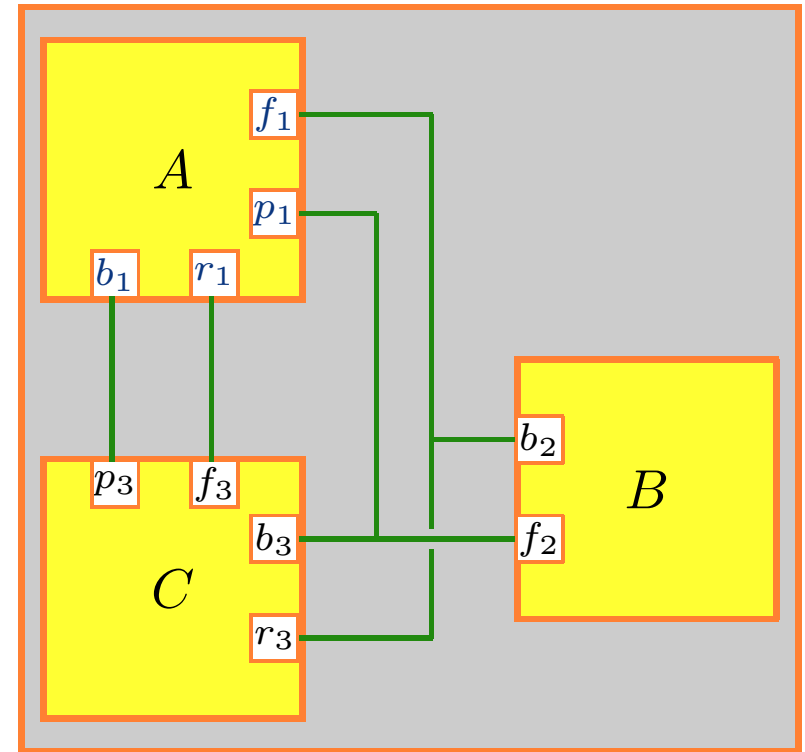
# Scope of the basic model

## Three layers:

1. Component behaviour
2. Coordination
3. Data transfer

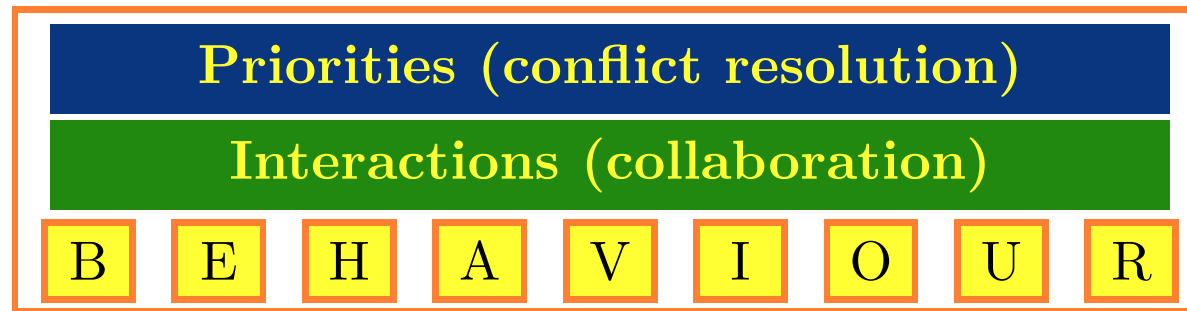
Interesting results already at this level, e.g.

- Analysis of synchronisation deadlocks
  - S. Bensalem, M. Bozga, J. Sifakis, T.-H. Nguyen. *D-Finder: A Tool for Compositional Deadlock Detection and Verification*. [CAV'09]
- Synthesis of glue for certain safety properties
  - S. Bliudze, J. Sifakis. *Synthesizing Glue Operators from Glue Constraints for the Construction of Component-Based Systems*. [Submitted to POPL'10]



# Basic model of BIP

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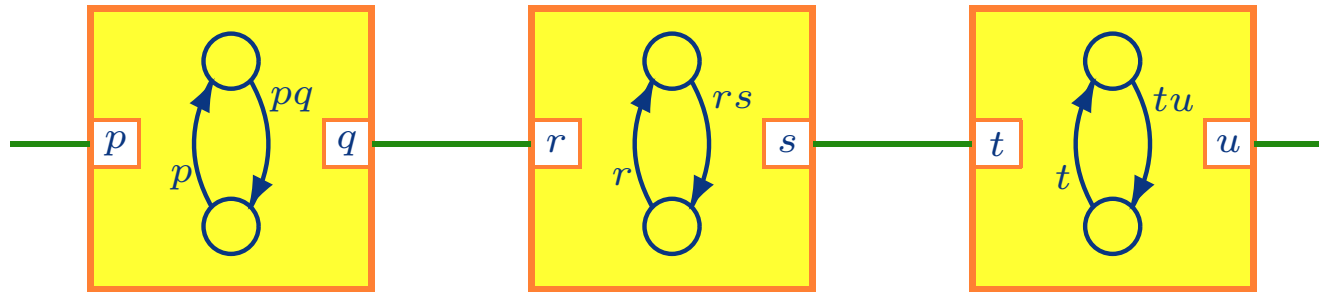


Layered component model

- **Behaviour** — labelled transition systems with **disjoint** sets of ports
- **Interaction** — set of interactions (interaction = set of ports)
- **Priorities** — strict partial order on interactions

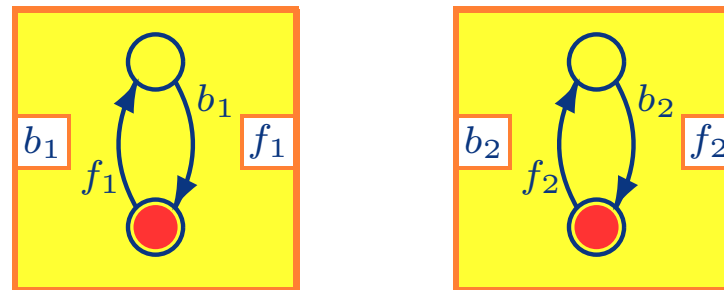
# BIP: Examples

## Modulo-8 counter:



Interactions:  $\{p, pqr, pqrst, pqrstu\}$ .

## Mutual exclusion:



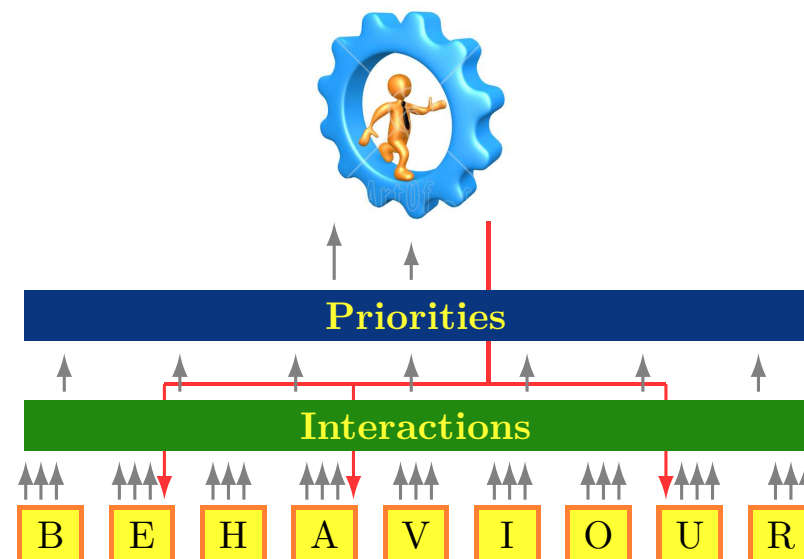
Interactions:  $\{b_1, f_1, b_2, f_2\}$

Priority:  $b_1 \prec f_2, b_2 \prec f_1$ .

# Implementation: Enumerative engine

## Engine protocol:

1. Atoms notify the engine of their active ports.
2. The engine enumerates the allowed interactions;
3. Filters out low priority ones;
4. Picks one among those left;
5. Notifies the atoms.



Interaction model is a **set of sets** of ports  $\Rightarrow$  exponential complexity.

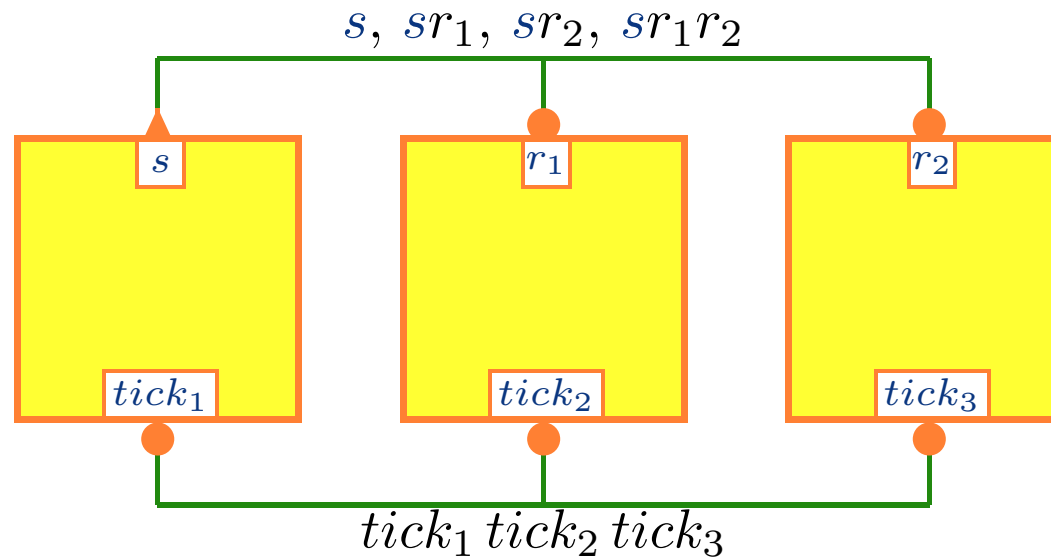
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- Boolean encoding
- Benchmarks

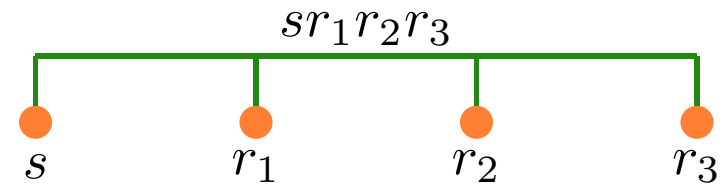
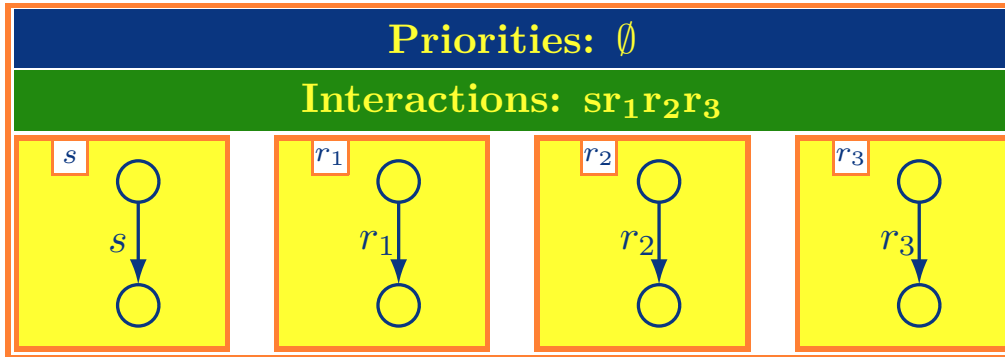
# Basic connectors

- A **connector** is a set of ports which can be involved in an interaction.
- Port attributes (**trigger** ▲, **synchron** ●) determine the synchronisation type.
- An **interaction** in a connector is a subset of ports such that either it contains a trigger or it is maximal.

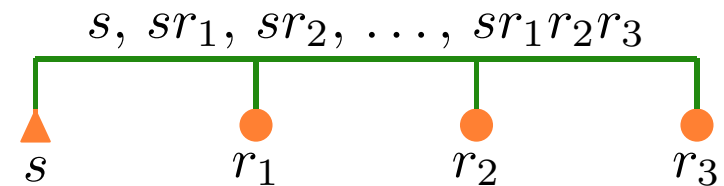
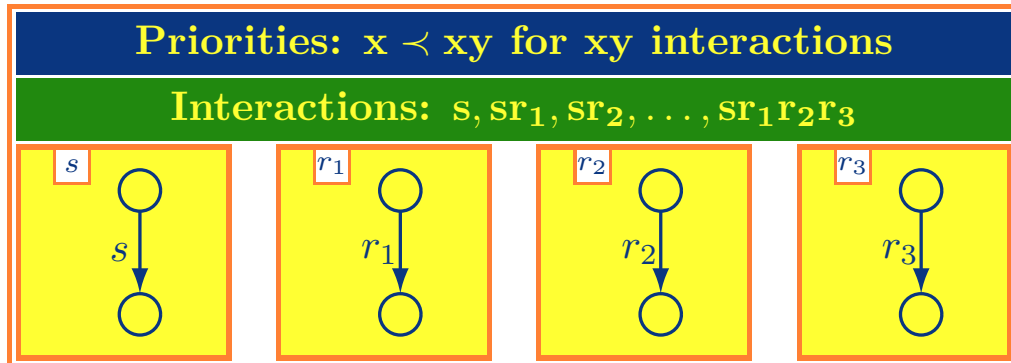


# Interaction modelling: Flat connectors

## Rendezvous

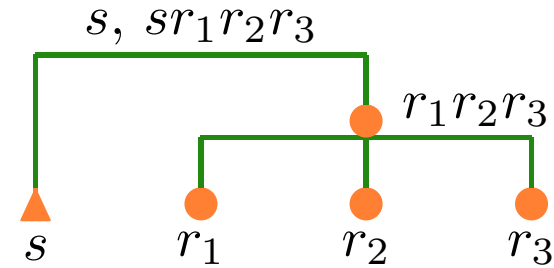
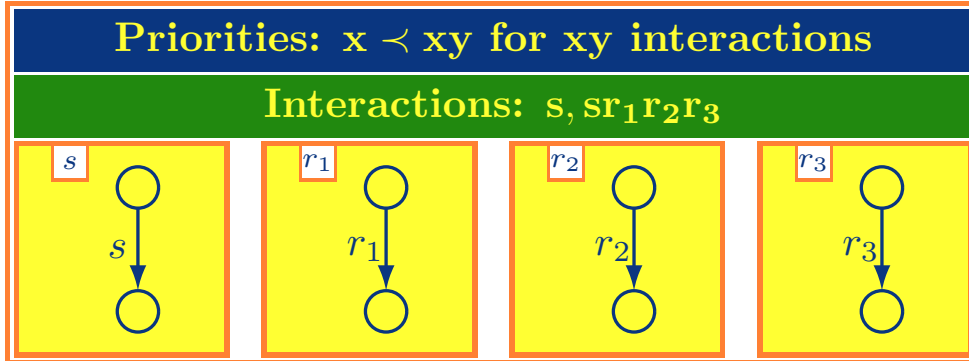


## Broadcast

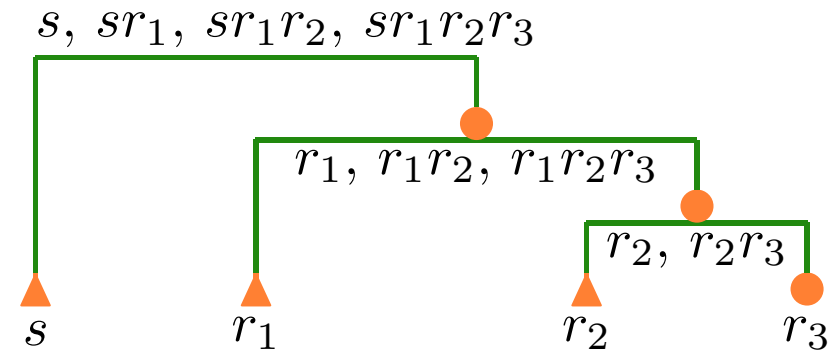
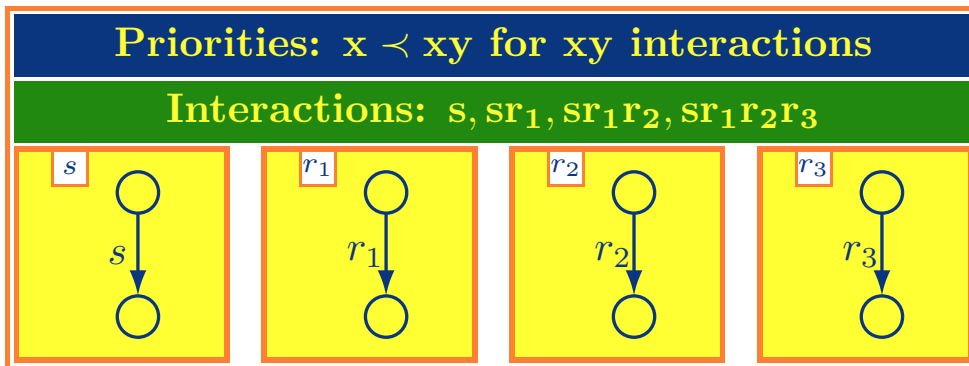


# Interaction modelling: Hierarchical connectors

## Atomic broadcast



## Causality chain



The Algebra of Connectors,  $\mathcal{AC}(P)$ , introduced in [EMSOF'T'07].



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# Symbolic implementation

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**Motivation:** Reduce Component/Engine protocol overhead.

**Approach:** Use boolean functions to pick the interaction to be executed.

- An interaction can be seen as a boolean valuation on ports:

$$p_1 p_2 \longleftrightarrow \begin{pmatrix} p_1 & p_2 & p_3 & p_4 \\ 1 & 1 & 0 & 0 \end{pmatrix}$$

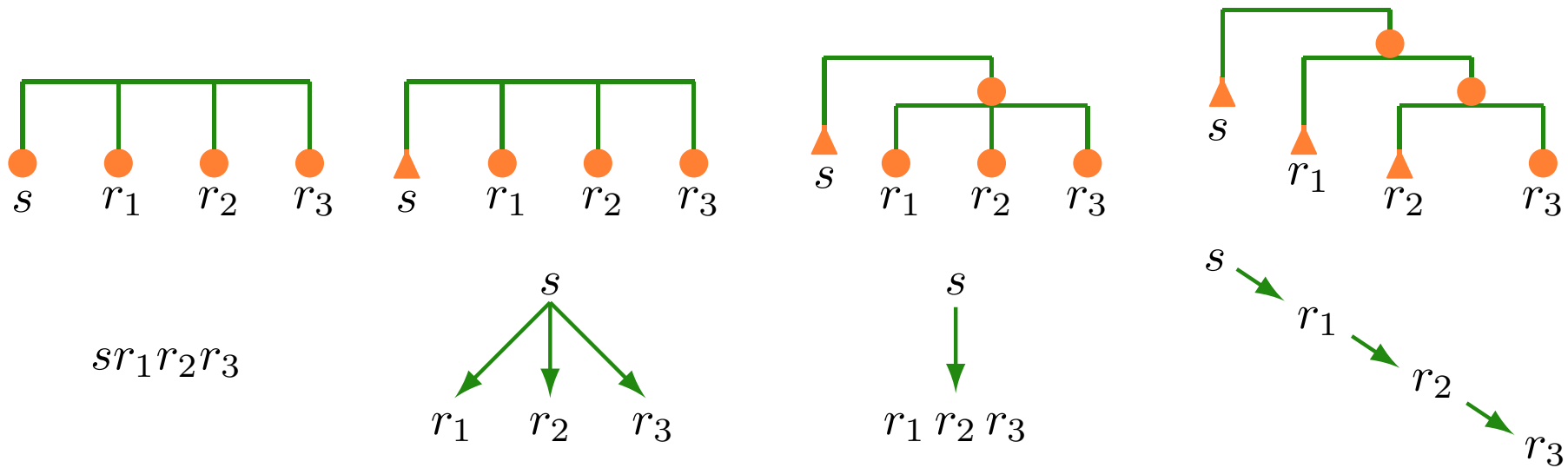
- Based on the connectors, priorities, and behaviour of components, compute a boolean formula  $\varphi$  on  $P \cup Q$ , such that

$$(a, q) \models \varphi \iff a \text{ is enabled in } q.$$

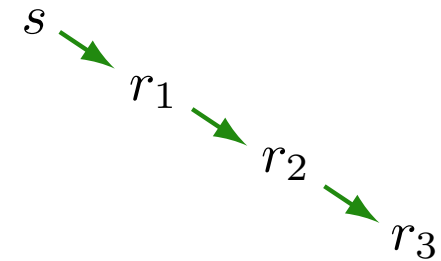
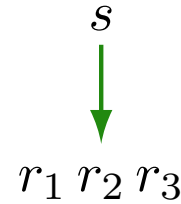
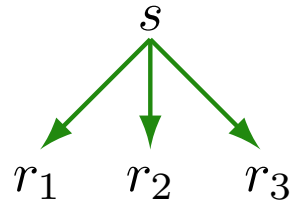
- Implementation using existing BDD package.



# Causal interaction trees



$sr_1r_2r_3$



*Rendezvous*

$sr_1r_2r_3$

*Broadcast*

$s, sr_1, sr_2, \dots$

$sr_2r_3, sr_1r_2r_3$

*Atomic broadcast*

$s, sr_1r_2r_3$

*Causal chain*

$s, sr_1, sr_1r_2,$

$sr_1r_2r_3$

**Transformations are straightforward in both ways.**

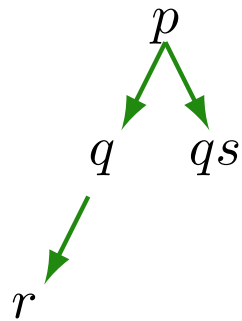
The Algebra of Causal Trees,  $CT(P)$ , introduced in [FMCO'07].



# Boolean representation of connectors

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$p'[q'r][qs]$ :



*Causal trees*

$true \Rightarrow p,$   
 $q \Rightarrow p,$   
 $r \Rightarrow pq,$   
 $s \Rightarrow pq$

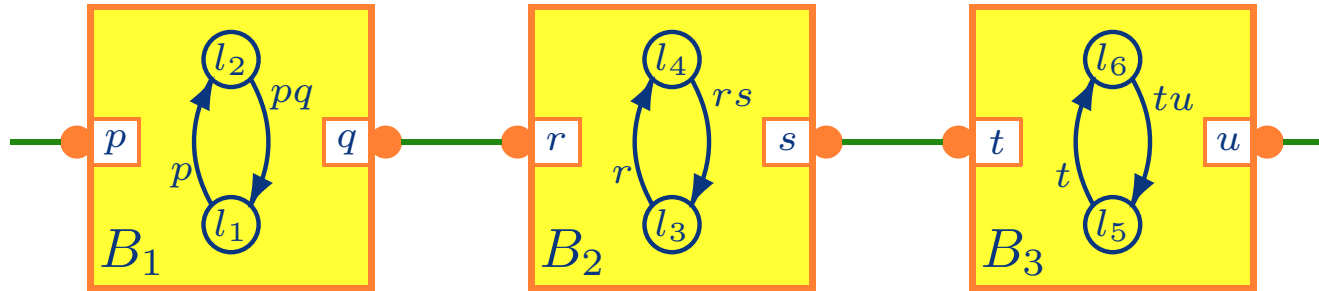
*Causal rules*

Notice that:  $(q \Rightarrow p \vee ps) \equiv (q \Rightarrow p)$ .

The corresponding boolean formula is

$$(true \Rightarrow p) \wedge (q \Rightarrow p) \wedge (r \Rightarrow pq) \wedge (s \Rightarrow pq) \equiv pq \vee p\bar{r}\bar{s}.$$

# Boolean representation of atomic components



$$f_{B_1} = l_1 \bar{l}_2 p \bar{q} \vee \bar{l}_1 l_2 p q \vee \bar{p} \bar{q}$$

$$f_B = (l_1 \bar{l}_2 p \bar{q} \vee \bar{l}_1 l_2 p q \vee \bar{p} \bar{q}) \wedge (l_3 \bar{l}_4 r \bar{s} \vee \bar{l}_3 l_4 r s \vee \bar{r} \bar{s}) \\ \wedge (l_5 \bar{l}_6 t \bar{u} \vee \bar{l}_5 l_6 t u \vee \bar{t} \bar{u})$$

$$f_C = (p \vee q r \vee s t \vee u) \wedge (q = r) \wedge (s = t)$$

# Implementation: Symbolic engine\*

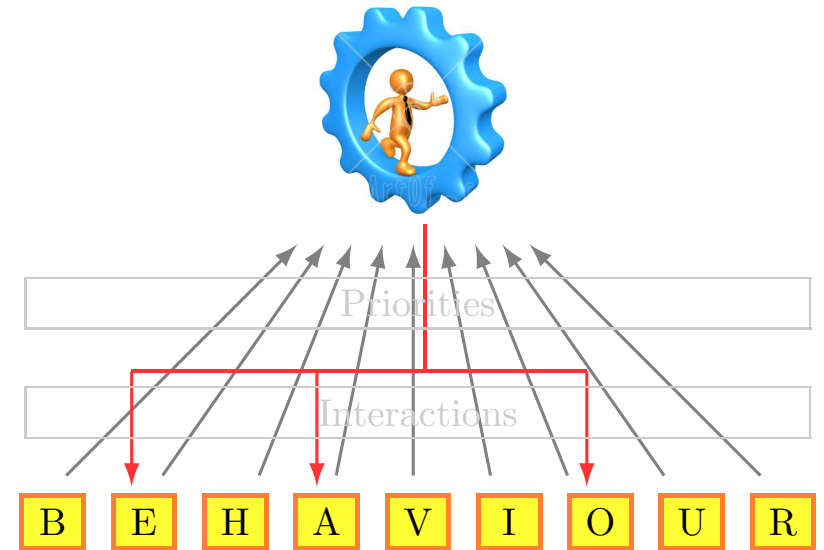
## Initialization:

0. The engine precomputes functions

$f_B \in \mathbb{B}[\bigcup_{i=1}^n Q_i, P]$  — behaviour,

$f_C \in \mathbb{B}[P]$  — connectors,

$f_S = f_B \wedge f_C$ .



## Engine protocol:

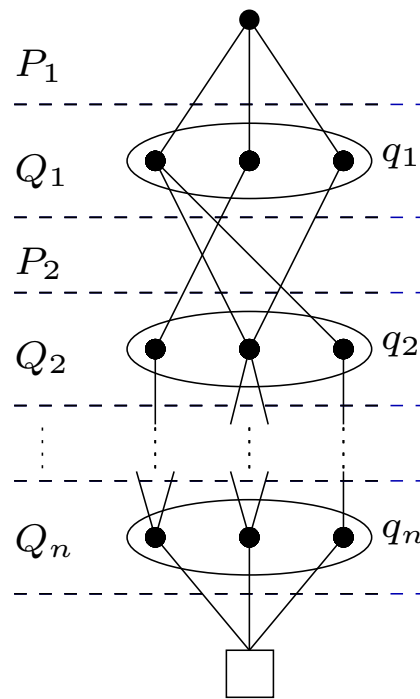
1. Atoms notify the engine of their current states  $q_i$ .
2. The engine picks any valuation  $a$  on  $P$ , such that

$$(a, q) \models f_S \wedge \bigwedge_{i=1}^n q_i$$

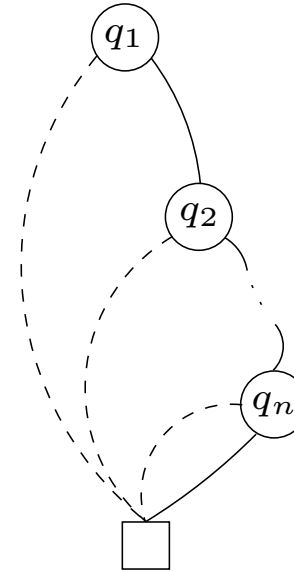
3. Notifies the atoms.

\* Connectors only (for priorities see in the paper).

# Complexity of the symbolic engine



$$f_S = f_B \wedge f_C$$



$$\bigwedge_{i=1}^n q_i$$

Complexity of the protocol:

- Conjunction  $f_S \wedge \bigwedge_{i=1}^n q_i : O(|f_S|)$  (sic!)
- Selecting  $a \models \dots : O(n)$ , where  $n = |P \cup Q|$ .

# Presentation outline

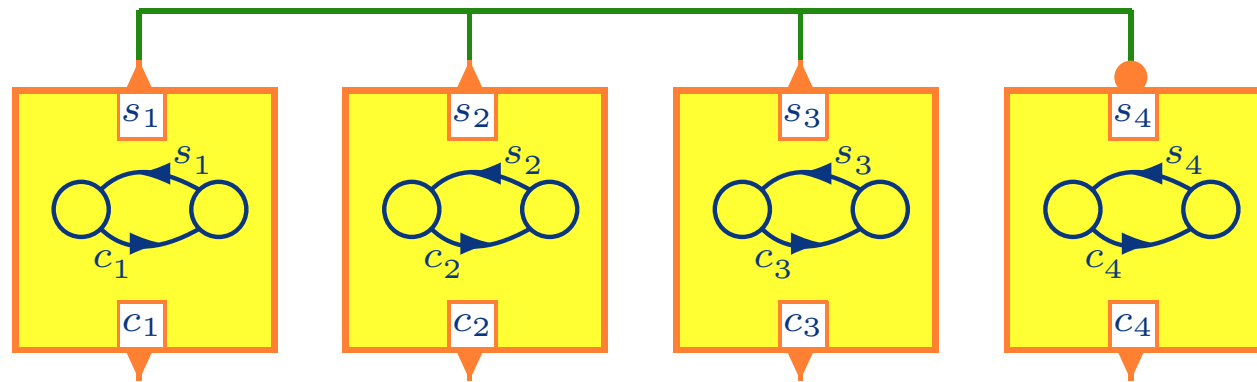
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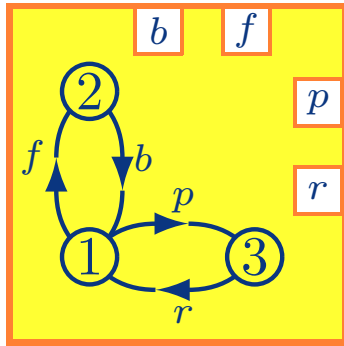
# Benchmarks: Bus

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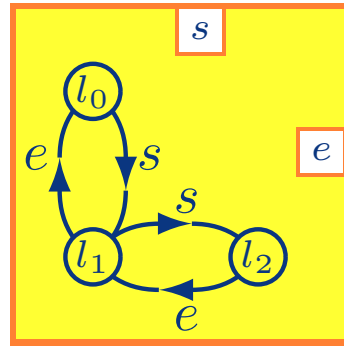


- $N$  clusters
- “Sparse” connectors:  $5N$
- Favours enumerative engine

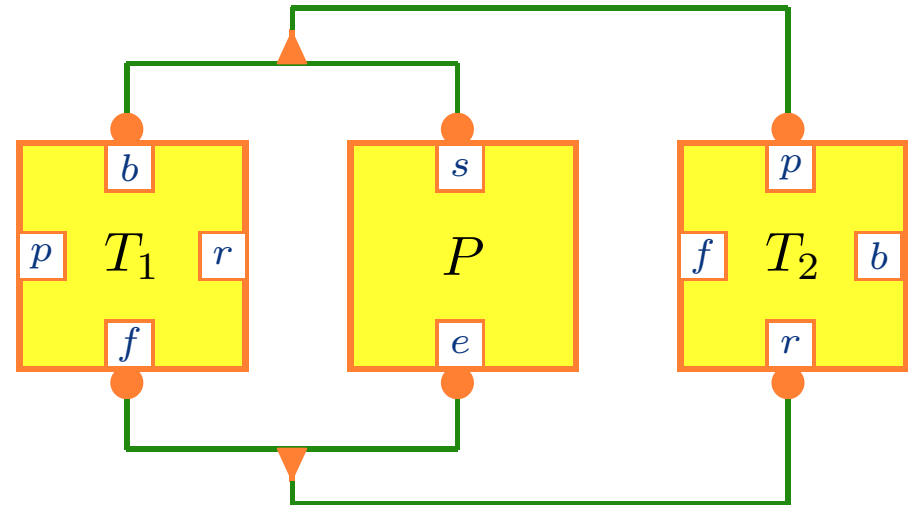
# Benchmarks: Preemptable tasks



*Task*



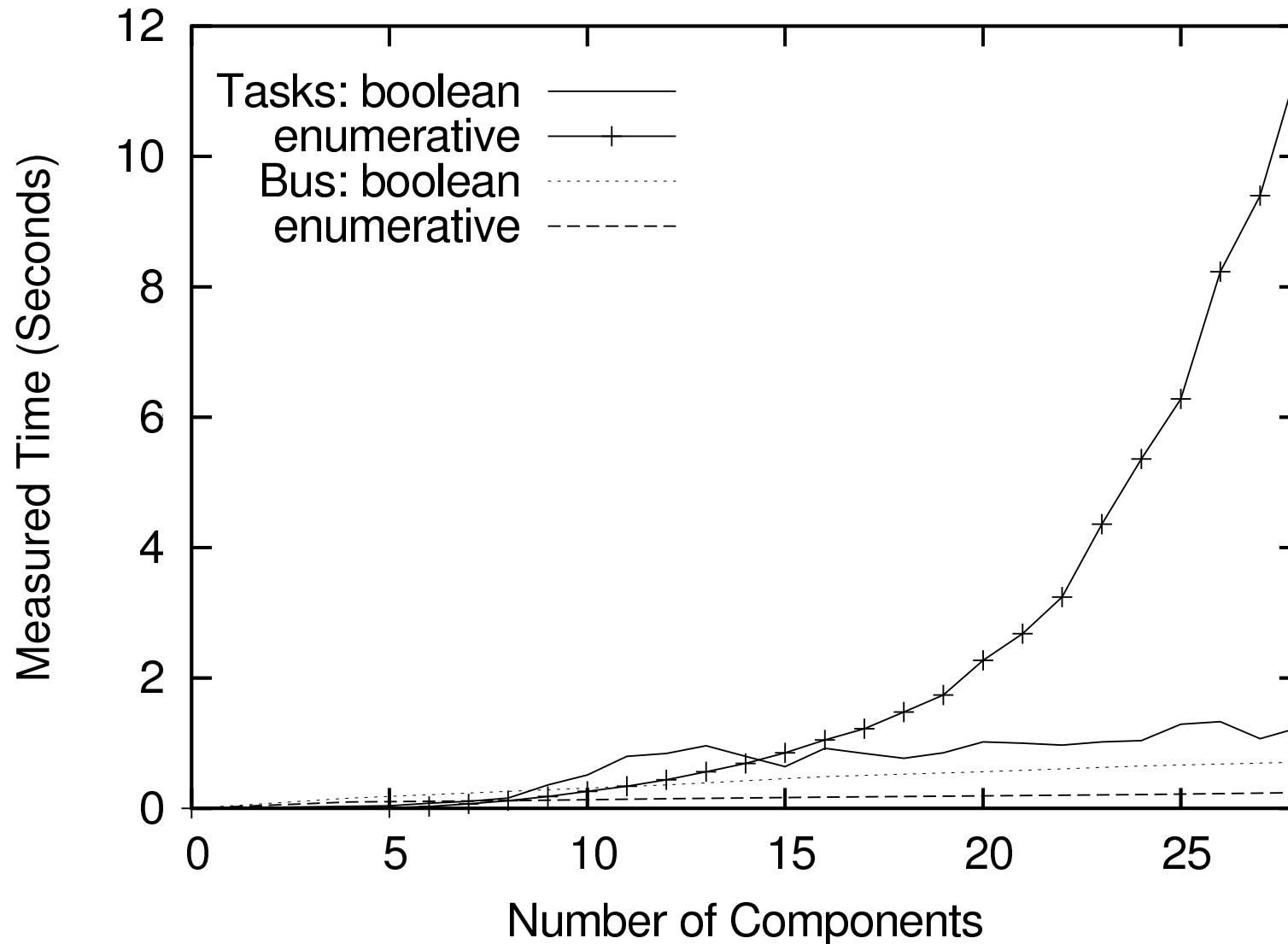
*Processor*



*Connectors*

- $N$  Tasks, 4 Processors
- “Dense” connectors:  $8N(N - 1)$
- Favours symbolic engine

# Benchmarks: Simulation results



# Conclusion

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- Symbolic engine implementation outperforms the enumerative one for “densly” connected systems.
  - How to characterize “dense”?
- BDD size linear in the number of components for both benchmarks.
  - Why? What about the general case?
  - Further optimizations, e.g. reordering components?
- Only one of the applications of the boolean representation:
  - Connector manipulation
  - Glue (connector & priority) synthesis



*Thank you for your attention!*

# The Algebra of Interactions $AI(P)$

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**Syntax:**  $x ::= 0 \mid 1 \mid p \mid x \cdot x \mid x + x \mid (x)$ , with  $p \in P$

**Axioms:**

- + union                      idempotent, associative, commutative, identity 0
- synchronisation      idempotent, associative, commutative, identity 1, absorbing 0  
   distributes over union

**Examples:**     $s + s r_1 + s r_2 + s r_1 r_2 = s(1 + r_1)(1 + r_2)$     broadcast  
    $s + s r_1 + s r_1 r_2 = s(1 + r_1(1 + r_2))$     causality chain



# The Algebra of Interactions $\mathcal{AI}(P)$

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**Semantics:** defined by the function  $\| \cdot \| : \mathcal{AI}(P) \rightarrow 2^{2^P}$

$$\|0\| = \emptyset,$$

$$\|1\| = \{\emptyset\},$$

$$\|p\| = \left\{ \{p\} \right\}, \text{ for any } p \in P,$$

$$\|x_1 + x_2\| = \|x_1\| \cup \|x_2\|, \text{ for any } x_1, x_2 \in \mathcal{AI}(P),$$

$$\|x_1 \cdot x_2\| = \left\{ a_1 \cup a_2 \mid a_1 \in \|x_1\|, a_2 \in \|x_2\| \right\}, \text{ for any } x_1, x_2 \in \mathcal{AI}(P).$$

# The Algebra of Connectors $AC(P)$

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## Syntax:

$s ::= [0] \mid [1] \mid [p] \mid [x] \quad (\textit{synchrons})$

$t ::= [0]' \mid [1]' \mid [p]' \mid [x]' \quad (\textit{triggers})$

$x ::= s \mid t \mid x \cdot x \mid x + x \mid (x)$

## Operators:

$+$  union idempotent, associative, commutative, identity  $[0]$

$\cdot$  fusion idempotent, associative, commutative, identity  $[1]$   
distributes over union ( $[0]$  is **not** absorbing)

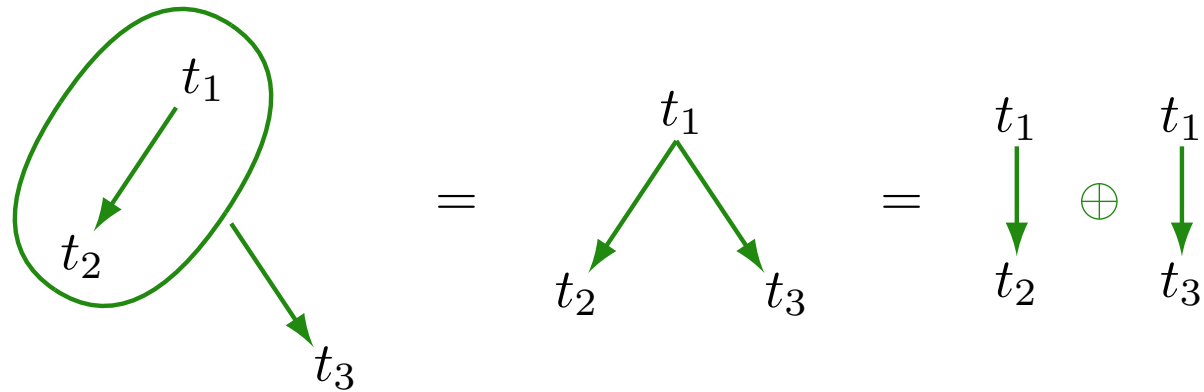
$[\cdot], [\cdot]'$  typing (often denoted  $[\cdot]^\alpha$  for some trigger/synchron typing  $\alpha$ )

**Semantics:** is given by a function  $|\cdot| : AC(P) \rightarrow AI(P)$ .

$$|p'qr| \stackrel{def}{=} p(1+q)(1+r)$$



# The Algebra of Causal Interaction Trees



**Syntax:**  $t ::= a \mid t \rightarrow t \mid t \oplus t.$

**Essential axioms:**

$$\begin{aligned} (t_1 \rightarrow t_2) \rightarrow t_3 &= t_1 \rightarrow (t_2 \oplus t_3), \\ t_1 \rightarrow (t_2 \oplus t_3) &= t_1 \rightarrow t_2 \oplus t_1 \rightarrow t_3, \\ (t_1 \oplus t_2) \rightarrow t_3 &= t_1 \rightarrow t_3 \oplus t_2 \rightarrow t_3. \end{aligned}$$

**Semantics:**  $|\cdot| : CT(P) \rightarrow AI(P)$

$$\begin{aligned} |a| &= a, \\ |a \rightarrow t| &= a(1 + |t|), \\ |t_1 \oplus t_2| &= |t_1| + |t_2| + |t_1||t_2| \end{aligned}$$

